

# *CS Applications in Graphics & Vision*

27 Colóquio Brasileiro de Matemática

## Outline

- Overview of Applications
  - How & Where to Use CS
- Hardware
  - Single-Pixel Camera
- Software
  - Light Transport Sensing

# The Good and Bad of CS

- Good:
  - Simultaneous Sensing & Compression
  - Minimal Non-Adaptive Measurements
  - Stable / Robust to Noise
- Bad:
  - Global Probing ~ *Special Devices*
  - Non-Linear Estimation ~ *Expensive Recovery*

## Where to Use CS?

- ▶ Massive (Sparse) Raw Data
- Hardware Options
  - Existing Suitable Devices (i.e., MRI, CT, etc..)
  - Data Parallel Acquisition (i.e., Sensor Networks)
  - New Analog-Digital Converters
- ✱ *Break Technological Limits*

# How to Use CS?

- Asymmetrical
  - Low Rate Sampling + Large Scale Optimization
- Universality
  - Representation Independent Sensing
- Model-Based Estimation
  - Dimensionality Reduction
- Operator Sparseness
  - Statistical Analysis / Processing

# Application Areas

- Biomedical Imaging
- Geophysics / Radar
- Astronomy
- Analog-Digital Converters
- Machine Learning
- Vision and Graphics

# Single-Pixel Camera

- ▶ Early Example of Dedicated CS Device

- <http://dsp.rice.edu/cscamera> (data)

- Rice University / DSP Group (2006)



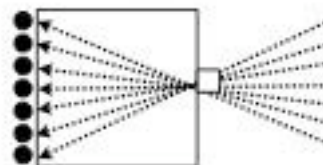
- MIT Technology Review: *Top 10 emerging technologies for 2007*



## Comparison

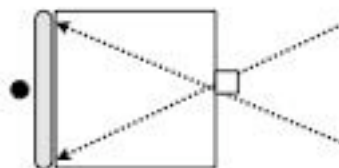
- Conventional Camera (CCD/CMOS array)

- Millions of Sensors (ray bundle per pixel)
- Space Multiplexed

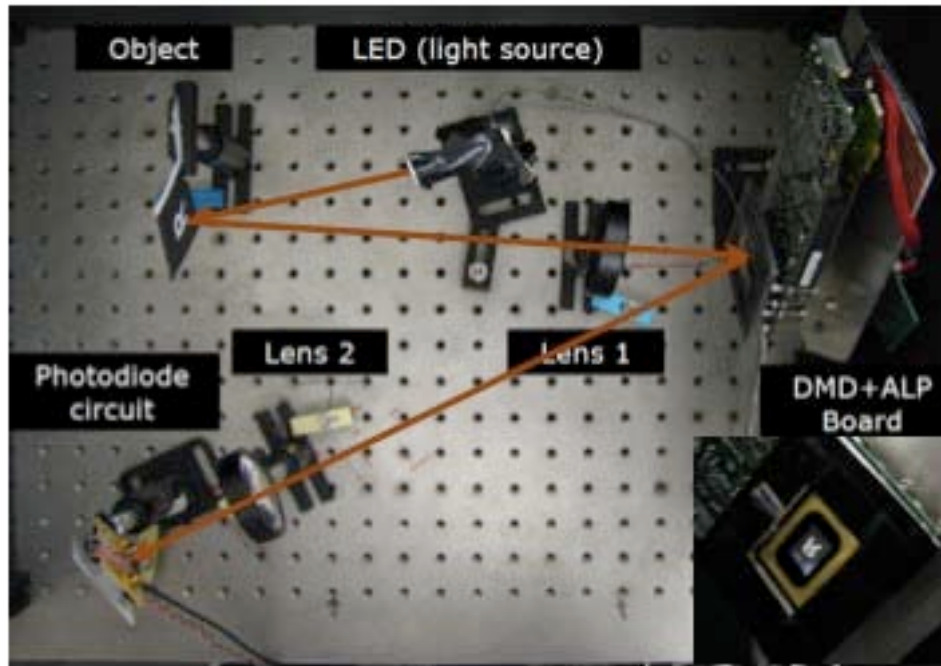


- CS Camera (CS integrator)

- One Sensor (all rays)
- Time Multiplexed

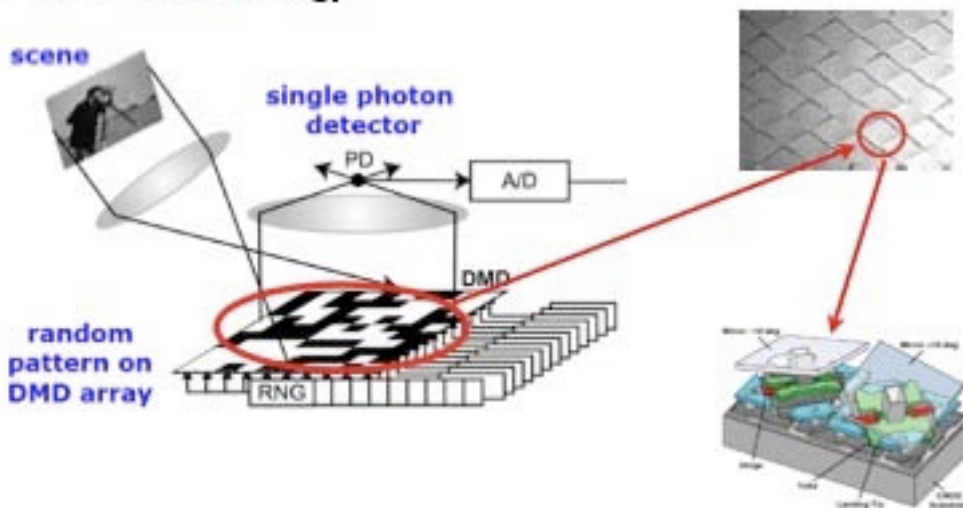


# Experimental Setup



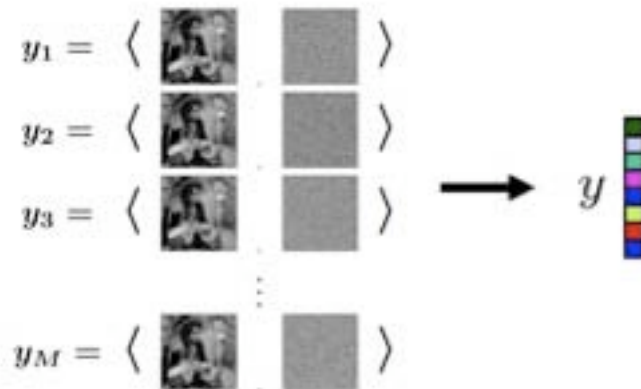
# CS Integrator

- DLP Technology



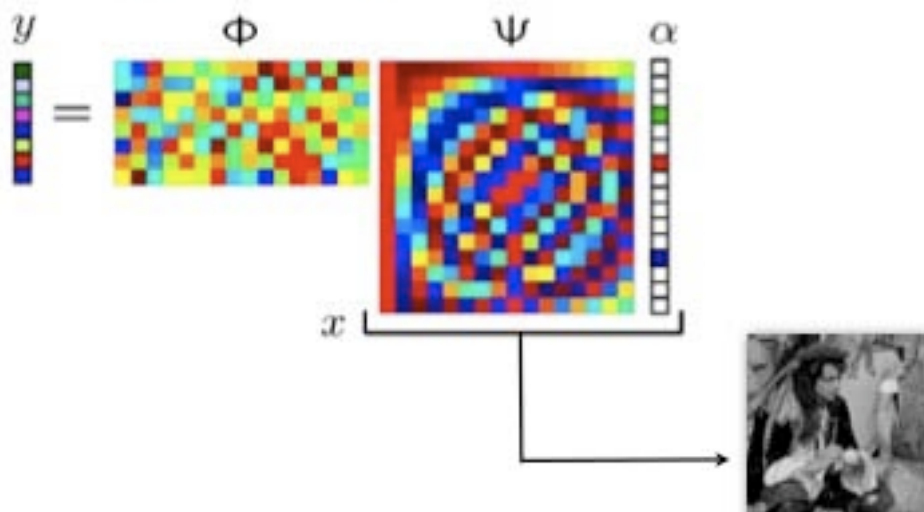
# Image Sensing

- Measurements in Time
  - Flip Mirrors  $M$  Times



# Image Recovery

- CS Optimization (TV)



# Example 1

- First Image Acquisition

target  
65536 pixels



11000 measurements  
(16%)



1300 measurements  
(2%)



# Example 2



4096  
pixels



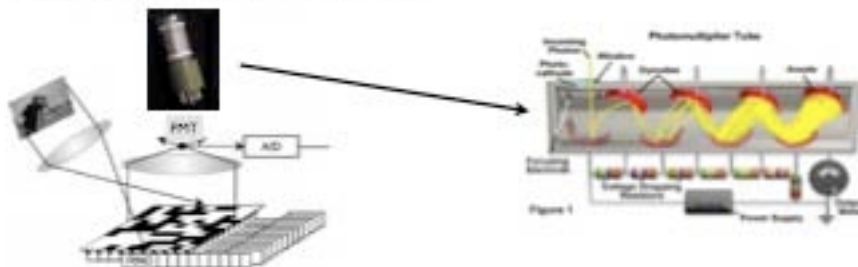
500  
random measurements

# Advantages

- When the sensor is expensive:
  - Low Light Imaging
  - High Dynamic Range
  - Hyperspectral Imaging
  - Shutterless Video
  - etc...

## Low-Light Imaging

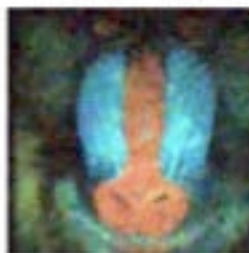
- Photomultiplier Tube



Mandrill 256x256



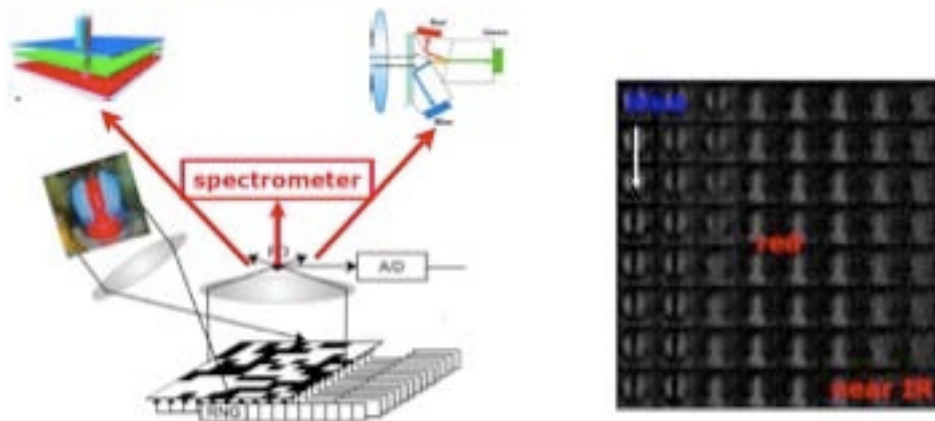
Mandrill 10x sub-Nyquist





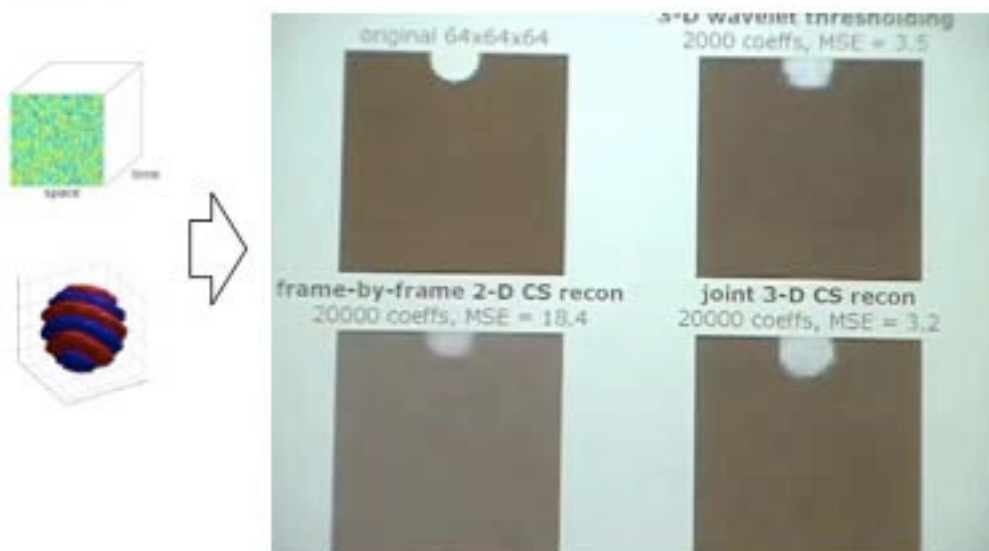
# Hyperspectral Imaging

- Layer Sensors (Multi-Photodiodes, etc)
- Prism Assembly



# Shutterless Video

- Space-Time Reconstruction (3D Wavelets)



# Dual Photography

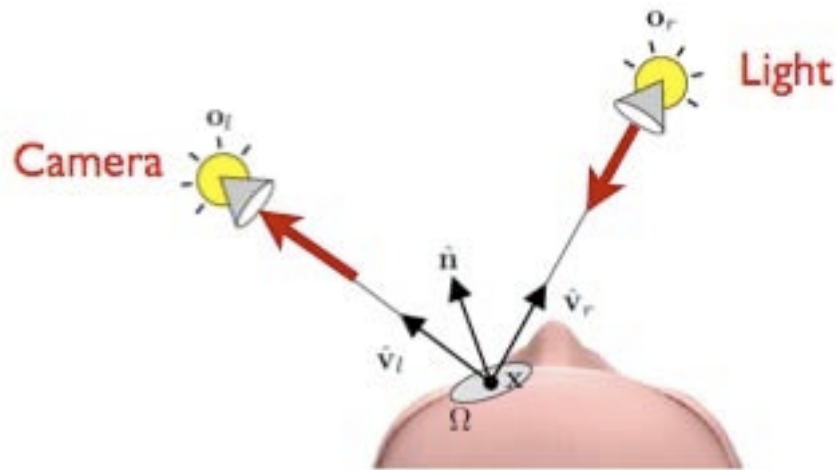
- The Reciprocity Principle
- Single Pixel Dual Camera
- Compressive Light Transport Sensing
- Relighting
- CS Dual Camera

## First Application in Graphics

- *Compressive Dual Photography*
  - Sen, P. and Darabi, S. - EUROGRAPHICS 2009
- *Compressive Light Transport Sensing*
  - Peers et al. - SIGGRAPH 2009
- *Compressive Structured Light for Recovering Inhomogeneous Participating Media*
  - Gu et al. - ECCV 2008

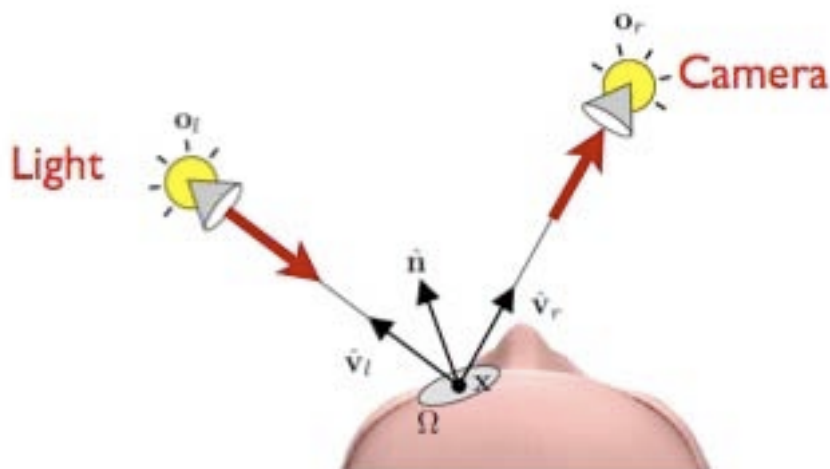
# The Reciprocity Principle

- Interchange Camera and Light  
(Helmholtz, 1856)



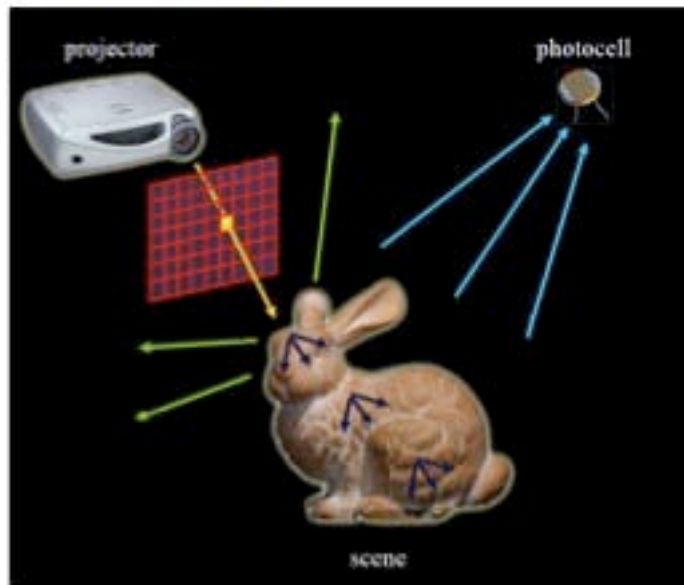
# The Reciprocity Principle

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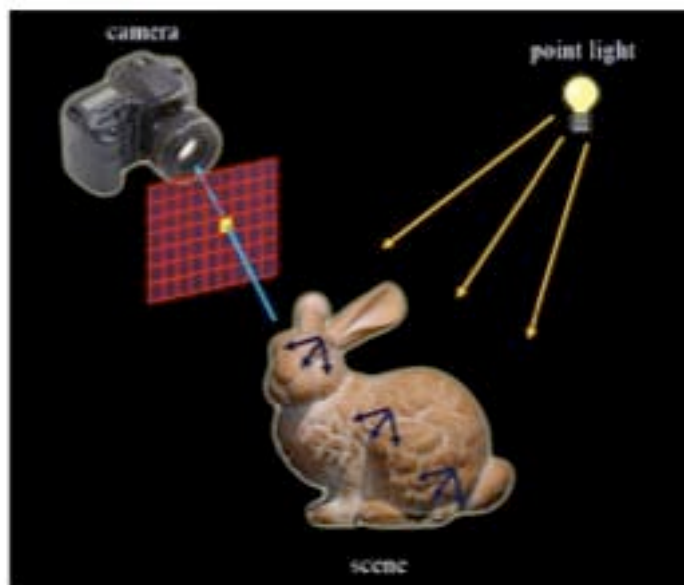
# Dual Single Pixel Camera

- Primal Configuration



# Dual Single Pixel Camera

- Dual Configuration



# Brute Force Acquisition

projector



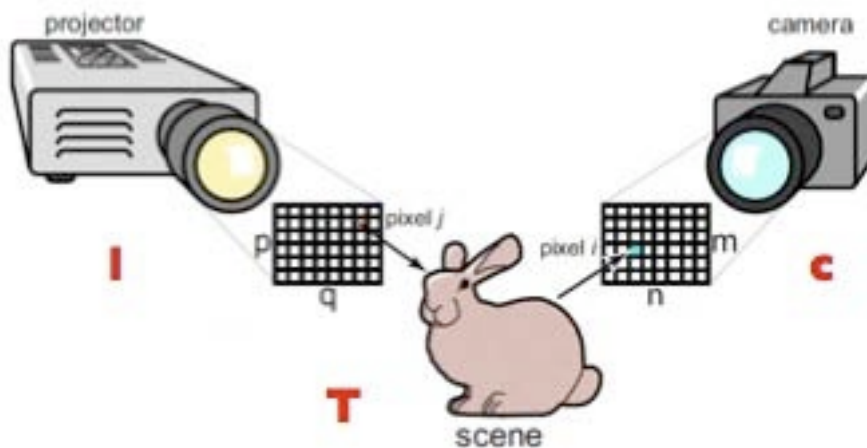
photosensor



scene

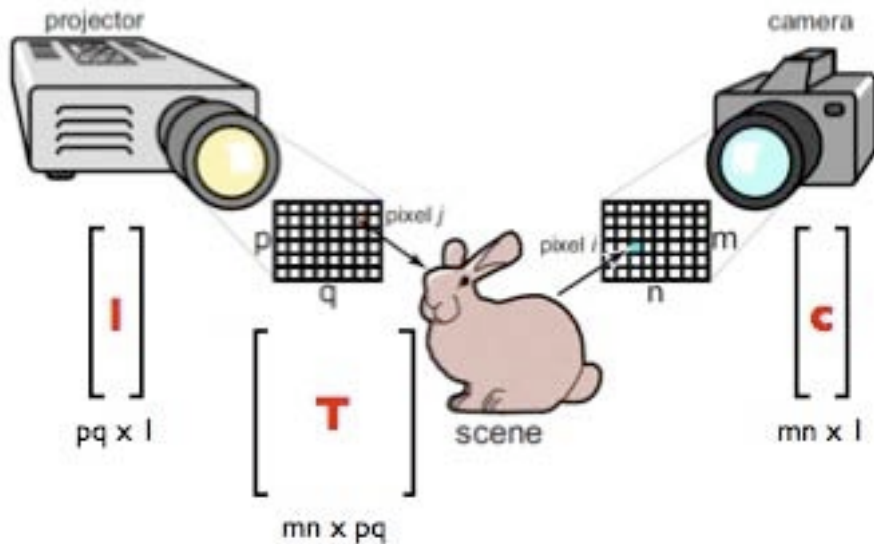
## 4D Light Transport

- Replace Photocell with a Camera



# 4D Light Transport Matrix

- Replace Photocell with a Camera



# The 4D Transport Matrix

- Primal Configuration

$$\begin{matrix} \mathbf{C} \\ \left[ \begin{array}{c} \text{shaded bar} \end{array} \right] \\ mn \times 1 \end{matrix} = \begin{matrix} \mathbf{T} \\ \left[ \begin{array}{c} \text{shaded bar} \end{array} \right] \\ mn \times pq \end{matrix} \begin{matrix} \mathbf{I} \\ \left[ \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \right] \\ pq \times 1 \end{matrix}$$

# The 4D Transport Matrix

- Primal Configuration

$$\begin{array}{c} \mathbf{c} \\ \left[ \begin{array}{c} \text{light pink bar} \\ \text{light pink bar} \\ \text{light pink bar} \\ \text{light pink bar} \\ \text{light pink bar} \end{array} \right] \\ mn \times 1 \end{array} = \begin{array}{c} \mathbf{T} \\ \left[ \begin{array}{cc} \text{dark pink bar} & \text{light pink bar} \\ \text{dark pink bar} & \text{light pink bar} \\ \text{dark pink bar} & \text{light pink bar} \\ \text{dark pink bar} & \text{light pink bar} \\ \text{dark pink bar} & \text{light pink bar} \end{array} \right] \\ mn \times pq \end{array} \begin{array}{c} \mathbf{I} \\ \left[ \begin{array}{c} 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{array} \right] \\ pq \times 1 \end{array}$$

# The 4D Transport Matrix

- Primal Configuration

$$\begin{array}{c} \mathbf{c} \\ \left[ \begin{array}{c} \text{dark pink bar} \\ \text{dark pink bar} \\ \text{dark pink bar} \\ \text{dark pink bar} \\ \text{dark pink bar} \end{array} \right] \\ mn \times 1 \end{array} = \begin{array}{c} \mathbf{T} \\ \left[ \begin{array}{ccc} \text{dark pink bar} & \text{light pink bar} & \text{dark pink bar} \\ \text{dark pink bar} & \text{light pink bar} & \text{dark pink bar} \\ \text{dark pink bar} & \text{light pink bar} & \text{dark pink bar} \\ \text{dark pink bar} & \text{light pink bar} & \text{dark pink bar} \\ \text{dark pink bar} & \text{light pink bar} & \text{dark pink bar} \end{array} \right] \\ mn \times pq \end{array} \begin{array}{c} \mathbf{I} \\ \left[ \begin{array}{c} 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{array} \right] \\ pq \times 1 \end{array}$$

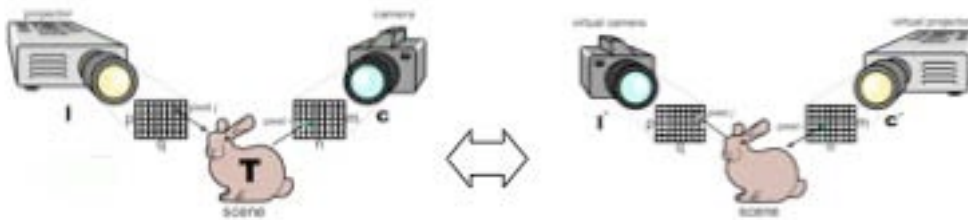
# Helmholtz Reciprocity

$$\mathbf{c} = \mathbf{T}\mathbf{l} \quad \Leftrightarrow \quad \mathbf{l}' = \mathbf{T}^t \mathbf{c}'$$

Primal

Dual

- Dual Photography

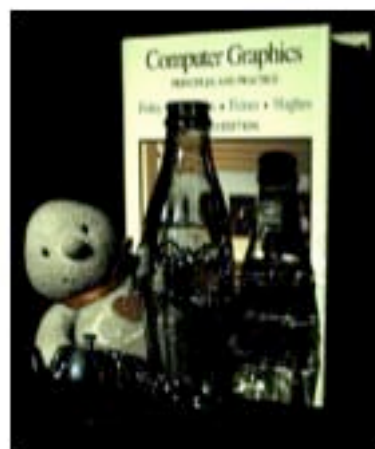


## Example 1

- (Sen et al., SIGGRAPH 2005)



Primal Photograph  
(projector is the light source)



Dual Image  
(as seen from projector)

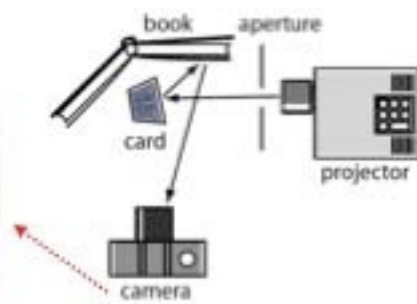


# Example 2

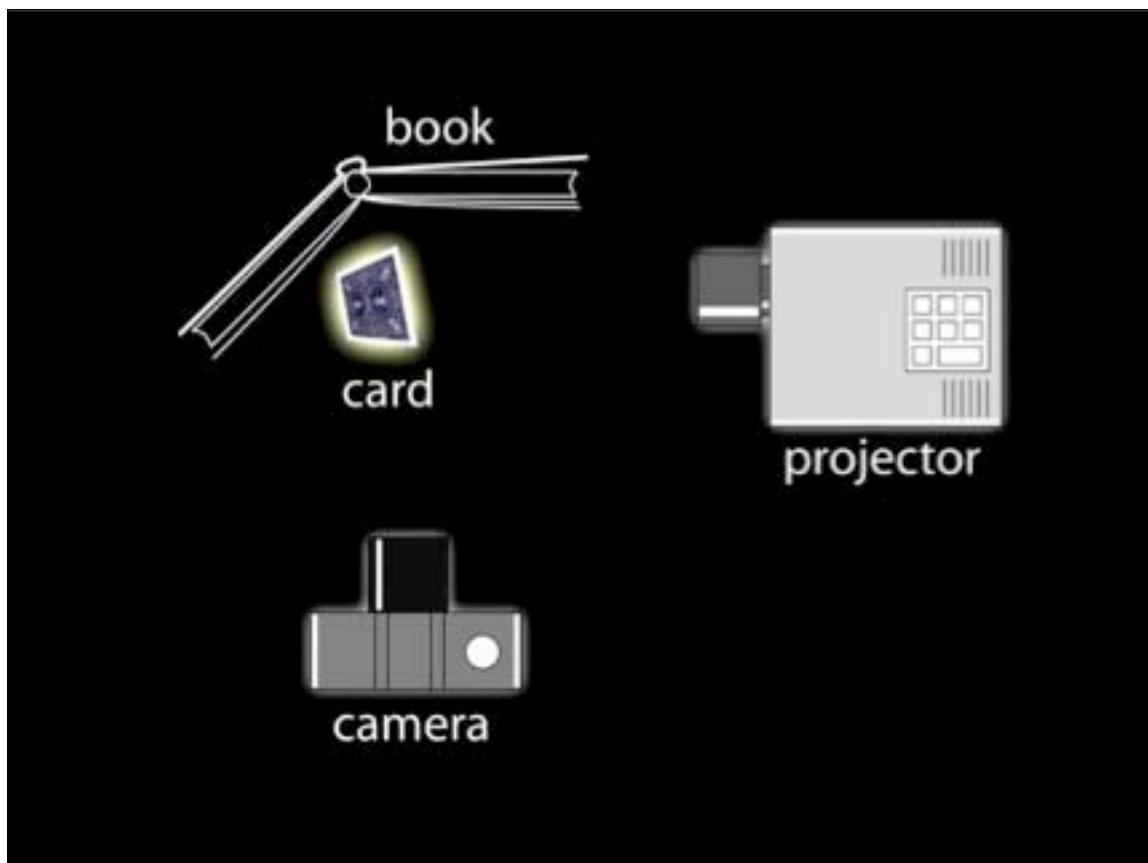
- Dual Photography from Diffuse Reflections



Camera's View



Projector's View



# Analysis

- Properties of the 4D Light Transport Matrix
  - little inter-reflection → sparse matrix
  - many inter-reflections → dense matrix
  - convex object → diagonal matrix
  - concave object → full matrix
- ▶ *How to Compute the Transport Matrix ?*

## Brute Force Approach

1. Project “Canonical Basis”
2. Capture Each Column of the Matrix

- Acquisition Costs

- Image / Projector Resolution:
  - ▶ 800 x 600 pixels = 480000 images
  - ▶ ~ 30 seg. / image = 4000 hours (167 days!)

\* *Not Feasible in Practice... (CS to the Rescue!)*

# CS Dual Photography

## ► *Compressive Light Transport Sensing*

- Few Non-Adaptive Measurements
- Sparsity Properties
  - Simple Scene and Lighting
    - Matrix  $\mathbf{T}$  Directly Sparse
  - Complex Scene and Lighting (columns of  $\mathbf{T}$  are images)
    - Sparse in the Wavelet Domain

## Sensing

### ● Light Transport Equation

$$\mathbf{C} = \mathbf{T}\mathbf{L}$$

### ● Brute Force ( $N$ images)

$$\begin{bmatrix} c_0 & \cdots & c_k \end{bmatrix} = \begin{bmatrix} \mathbf{T}_{n \times n} \end{bmatrix} \begin{bmatrix} 1 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & 1 \end{bmatrix}$$

### ● Compressive Sensing ( $K$ images, i.e, $K \ll N$ )

$$\begin{bmatrix} c_0 & \cdots & c_k \end{bmatrix} = \begin{bmatrix} \mathbf{T}_{n \times k} \end{bmatrix} \begin{bmatrix} l_0 & \cdots & l_k \end{bmatrix}$$

# The Recovery Trick

- Must Relate

- Light Transport Equation

$$C = TL$$

- to

- Compressive Sensing Equation

$$\min \|x\|_{\ell_1}$$

$$y = Ax$$

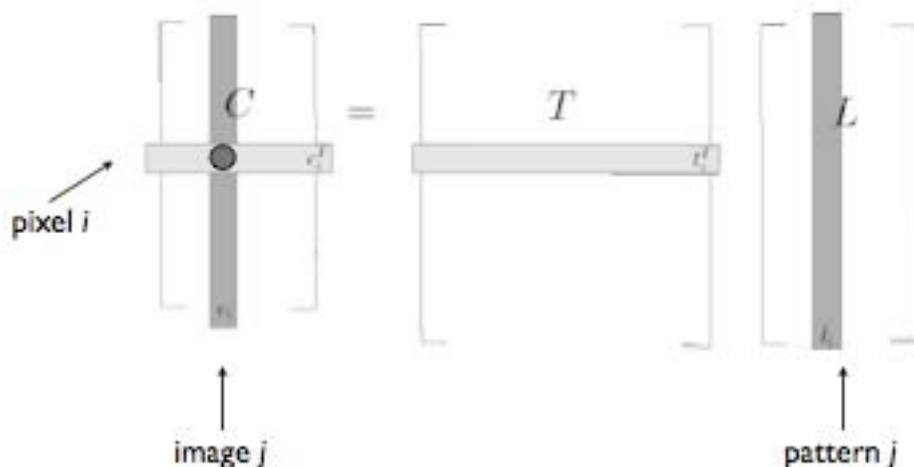
matrix

unknowns

vector

## Recovery: Step I

- Single Pixel through Time



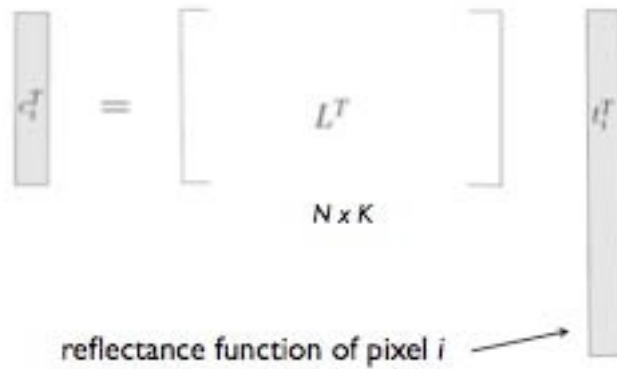
# Recovery: Step II

- Transpose Equation

$$C^t = L^t T^t$$

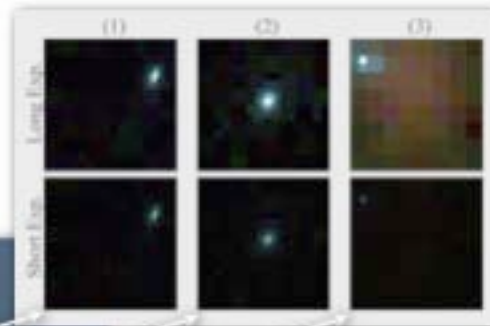
- Solve for each pixel

$$c_i^t = L^t t_i^t \quad \text{for } i = 1, \dots, K$$



# Reflectance Functions

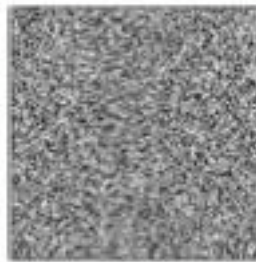
- (Peers et al., 2009)



# Implementation Details

- Matrix  $L$

- Sparse  $T \rightarrow L = \Phi$   
(i.e., Bernoulli Matrix)
- Dense  $T \rightarrow L = \Phi\Psi$   
(i.e., Daubechies Wavelets)

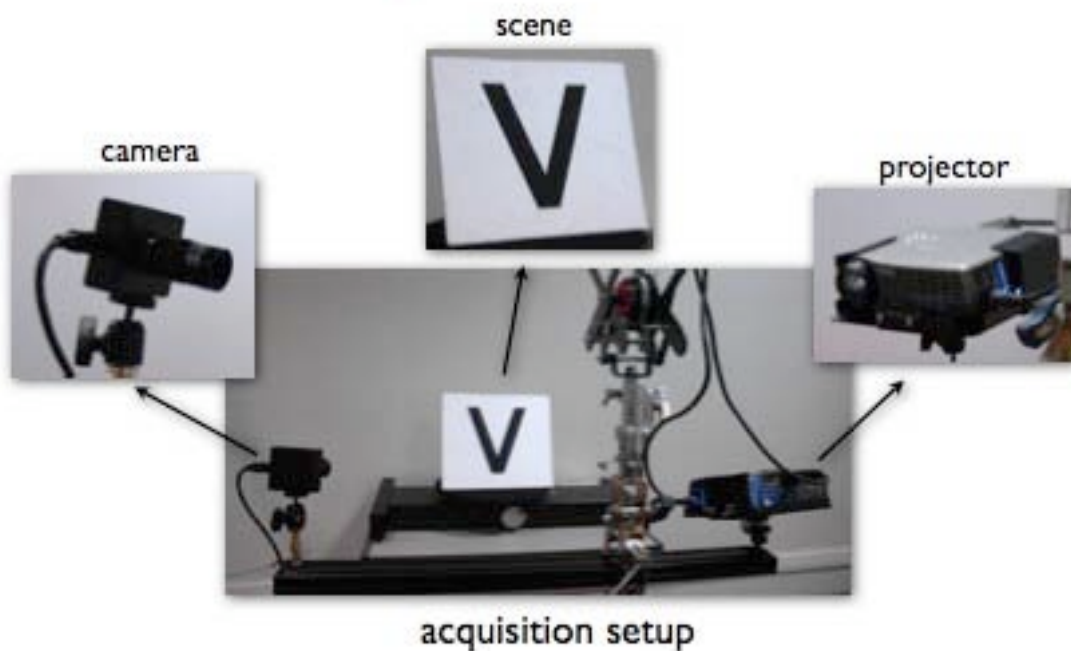


- Optimization Algorithm

- ROMP (Regularized Orthogonal Matching Pursuit)

► *OBS: Solve in Parallel for each pixel !!!*

# Experiments



# camera, lights, .. action!



## Images

- Projected Pattern

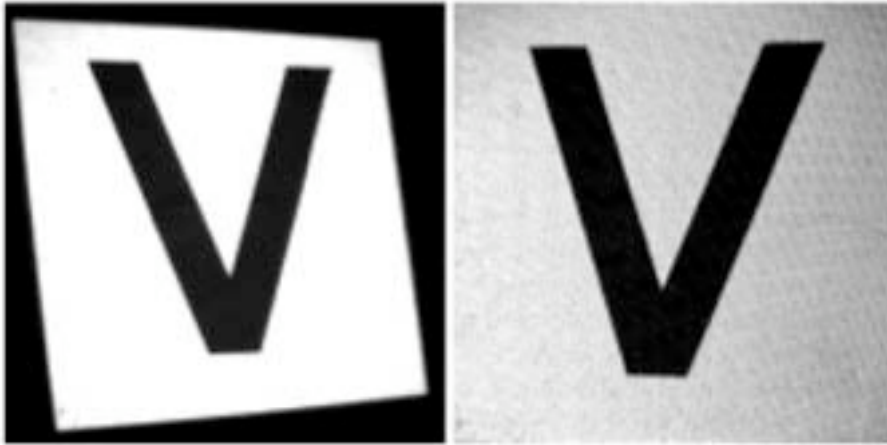


from the camera



from the projector

# Results I

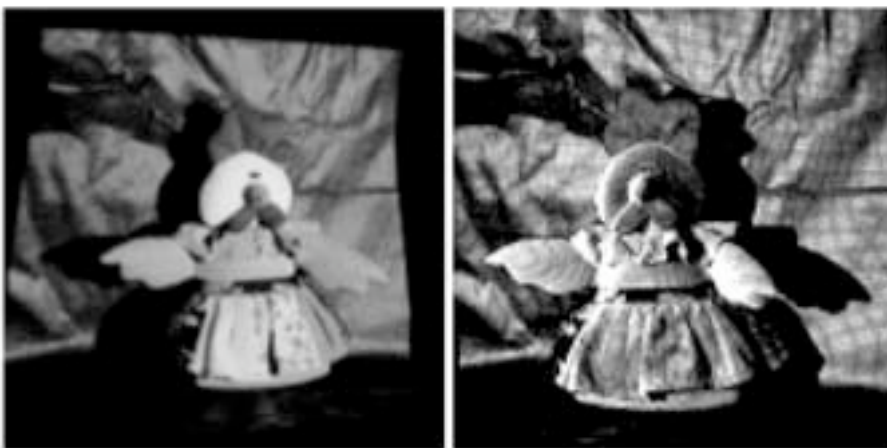


(a) Primal image.

(b) Dual image.

Figure: Image of size  $128 \times 128$ , captured with 1500 patterns.

# Results II



(a) Primal Image

(b) Dual Image

Figure: Image of size  $128 \times 128$ , captured with 1000 patterns.



# Results III-a



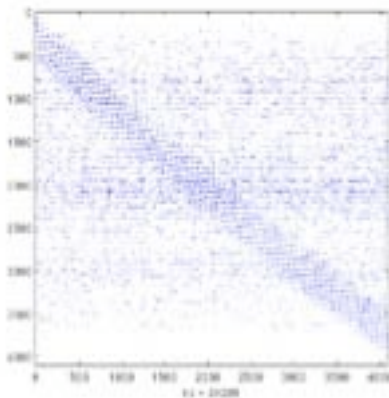
(a) 800 patterns



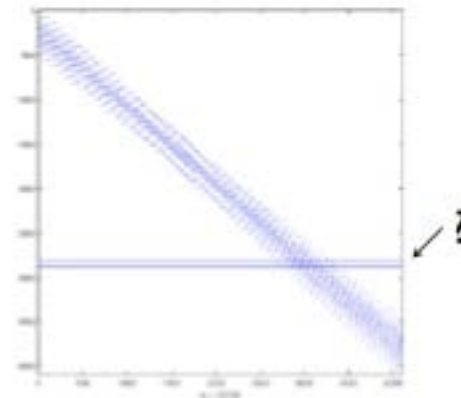
(b) canonic base

Figure: Image of size  $64 \times 64$ .

# Results III-b



(a) 800 patterns



(b) canonic base

Figure: Image of size  $64 \times 64$ .

# Image-Based Relighting

- Pipeline:

1. Measure 4D Light Transport Matrix  $\mathbf{T}$

$$\mathbf{C}^t = \mathbf{L}^t \mathbf{T}^t$$

2. Synthesize Incident Light Field  $l'$

$$l' = f(p)$$

3. Relight Scene with Transport Matrix

$$c' = \mathbf{T}l'$$

## Relighting I

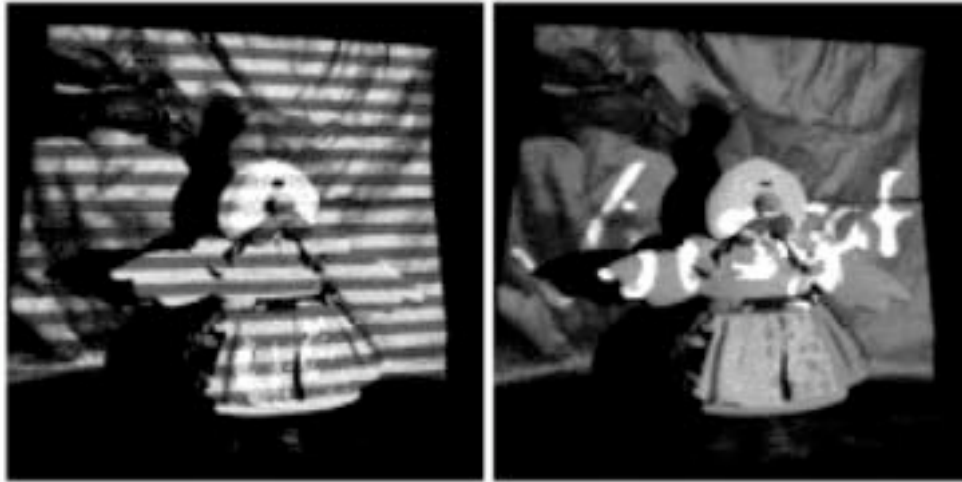
- (Schulz, et al., 2009)



(a) Image Relighting    (b) Image Relighting    (c) Image Relighting

Figure: Image of size  $128 \times 128$ , captured with 1500 patterns.

# Relighting II



(a) Image Relighting

(b) Image Relighting

Figure: Image of size  $128 \times 128$ , captured with 100 patterns.

## Dual CS Single Pixel Camera

- Use Camera as a Photocell
  - Integrate over All Image Pixels

$$c = \sum_j c_j$$

- Solve using Wavelet basis

$$c = \mathbf{L}^t \Psi^t \hat{t}$$

- Reconstruct

$$t = \Psi^t \hat{t}$$

# Example

- Comparison: Dual Single Pixel x Full DLT



15%, MSE: 35.9    25%, MSE: 27.2    40%, MSE: 13.1



50%, MSE: 8.8    75%, MSE: 7.9    100%



MSE: 7.3

Full DLT  
(512 patterns)

Image Resolution: 128 x 128 (16.384)

# Conclusions

- to be continued...